

#### SOUTH EAST ASIAN MATHEMATICAL SOCIETY

## **FINAL REPORT**

# Partial differential equations for image processing: theory and numerics

Nakhon Pathom, Thailand January 3 – 12, 2018

Organized by

Department of Mathematics, Silpakorn University, Thailand

### with the support of

Centre International de Mathématiques Pures et Appliquées South East Asian Mathematical Society International Mathematical Union Center for Promotion of Mathematical Research in Thailand Silpakorn University University of Picardie Jules Verne, LAMFA CNRS, France University of Évora, Portugal University Aberta, Portugal Centre of Mathematical Analysis, Geometry and Dynamical Systems, IST Portugal

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#### I. Summary

In this school, we introduced some basis of the theoretical and numerical mathematical analysis to study partial differential equations arising in image processing. Theoretical lectures were complemented by practical sessions through scientific Python software.

A website and a chat group were created to facilitate exchanges between students, lecturers and organizers. A drive, accessible directly from the website of the school, contains the lectures, the python script and the list of exercises.

Website https://sites.google.com/site/seamsthailand2018

Drive <u>https://sites.google.com/site/seamsthailand2018/documents</u>

#### II. Scientific Objectives and Rationale for the School

The area of numerical analysis in Thailand is well developed on the fixed point theory and optimization. Applications of numerical techniques to handle real world problems can be scarcely found. The Department of Mathematics at the Silpakorn University aims to create a young researchers group from ASEAN community to work on both the numerical analysis and its applications, especially the numerical methods in image processing.

This school was the first active SEAMS school concerning numerical analysis and scientific computing of partial differential equations in Thailand. It testifies the ability of the Silpakorn Dept. of Mathematics to participate in South East Asia (ASEAN) cooperation.

After the school, the Silpakorn University joins the European-Asian network launched by Prof. Joaquim Correia through the Erasmus+ call (enrolling by now, in Asia, Laos, Thailand, Vietnam, Philippines and India, in Europe, Scotland, France and Portugal).

#### III. Organizers and Lecturers

#### Scientific coordinators:

1. Name	:	Mrs Pornsarp Pornsawad	
Institution	:	Silpakorn University, Nakhon Pathom, Thailand	
Email and Phone : porn +66-		pornsawad_p@silpakorn.edu +66-34-245320	
2. Name	:	Mr Youcef Mammeri	
Institution	:	University of Picardie, Amiens, France	
Email and Phone		youcef.mammeri@u-picardie.fr +33-3-22827605	
3. Name	:	Mr. Joaquim Correia	
Institution	:	University of Évora, Évora, Portugal	
Email and Phone		jmcorreia@uevora.pt +351-91-7806756	

#### Local organizers:

The department of mathematics of Silpakorn university hosts the school. Local staff and students were involved to make this event a great success.

Mr. Worakrit Supaporn, PhD Mrs. Wannapa Panitsupakamon, Assistant Professor Miss Sawanya Sakuntasathien, PhD Mr. Supap Kirtsaeng, PhD Mr. Jittisak Rakbud, PhD Miss Nairat Kanyamee, PhD Miss Tiwadee Musunthia, PhD, Assistant Professor Miss Tammatada Khemaratchatakumthon, PhD Mr. Sittisede Polwiang, PhD Miss Passawan Noppakaew, PhD Miss Sineenuch Suwannaphichat, PhD Mrs. Parichat Srathongshoum, Staff Mrs. Gingdao Sarajoum, Staff

Miss Parada Sungcharoen, Master Student Mr. Naeem Binibroheng, Master Student Mr. Kitipong Thangsi, Master Student Mr. Kitipong Subwattanachai, Undergraduate Student Miss Phitchapha Lertsiravarameth, Undergraduate Student Miss Rangsima Traiwet, Undergraduate Student Miss Charatphon Phatchoun, Undergraduate Student Miss Thongkorn Raksantinana, Undergraduate Student Miss Sitranoot Pummiprakai, Undergraduate Student Miss Arunya Klaypothong, Undergraduate Student Miss Monthicha Noibanlat, Undergraduate Student Miss Pornpimon Sroisangwan, Master Student Miss Chanapat Suttipan, Master Student Miss Pitchaporn Paitong, Master Student

#### Lecturers:

Five international lecturers, accompanied by a doctor from the host University (who is a PhD from UK), ensured the lessons. Two assistants from Silpakorn University and two assistants from the National University of Laos were giving a hand up. We had the opportunity to loop Professor Fernando da Costa from University Aberta (Portugal). He is a world recognized researcher and valuable teacher. We decide to share the lecture of Prof. Nabil Bedjaoui and it was really appreciated by the students.

1. Mr Noppadol CHUMCHOB, PhD, Silpakorn University, Thailand Assistant professor <u>https://www.researchgate.net/profile/Noppadol\_Chumchob</u> <u>chumchob\_n@silpakorn.edu</u>

2. Ms Marília PIRES, PhD, University of Évora, Portugal Assistant professor <u>http://www.dmat.uevora.pt/pessoas/(id)/26227</u> <u>marilia@uevora.pt</u>

3. Mr Joaquim CORREIA, PhD, University of Évora, Portugal Assistant professor <u>http://www.dmat.uevora.pt/pessoas/(id)/5348</u> <u>jmcorreia@uevora.pt</u>

4. Mr. Fernando Pestana da COSTA, PhD with Agregação, University Aberta, Portugal Associate professor <u>https://www.math.tecnico.ulisboa.pt/~fcosta/</u> fernando.costa@uab.pt

5. Mr Nabil BEDJAOUI, PhD, University of Picardie, Amiens, France Maître de conferences <u>https://www.researchgate.net/profile/Nabil\_Bedjaoui</u> <u>nabil.bedjaoui@u-picardie.fr</u>

6. Mr Youcef MAMMERI, PhD, HDR, University of Picardie, Amiens, France Maître de conferences HDR http://www.lamfa.u-picardie.fr/mammeri youcef.mammeri@u-picardie.fr

#### IV. The Participants

50 participants were present during this SEAMS school, among them 24 non-Thai (coming from India, Indonesia, Myanmar, Philippines, Vietnam, Laos and Cambodia) and 26 Thai. We note that 24 are females and 26 males.

Name	Address	Gender

#### Foreign participants

1	Surojit Biswas	jit Biswas IIT Kharagpur, India		
2	Saheb Dalapati	IIT Bhubaneswar, India	М	
3	Anggia	Institut Teknologi Bandung, Indonesia	F	
4	Vanessa Sutandar	Institut Teknologi Bandung, Indonesia	F	
5	Saw Win	University of Mandalay, Myanmar	М	
6	Airish Pelemeniano	Caraga State University, Philippines	F	
7	Cheryl Quindao-Mentuda	Caraga State University, Philippines	F	
8	Tran Dinh Phung	Quy Nhon University, Vietnam	М	
9	Bouasy Doungsavanh	National University of Laos	F	
10	Bounmy Khaminsou	National University of Laos	М	
11	Gnord Maypaokha	National University of Laos	F	
12	Kedtysack Xayxanadasy	National University of Laos	М	
13	Khankham Vongsavang	National University of Laos	М	
14	Lisatteur Lilianou	National University of Laos	М	
15	Phoui Souksomvang	National University of Laos	М	
16	Latsamy Phonesay	Savannakhet University, Laos	М	
17	Saysamone Saiyasand	Savannakhet University, Laos	М	
	Sirixay			
18	Somphonephachan	Savannakhet University, Laos	М	
19	Somsanith Sithtisak	Savannakhet University, Laos	М	
20	Thongma Keomanivong	Savannakhet University, Laos	М	
21	Mettachit Sengsouly	Savannakhet University, Laos	F	
22	Thotsakanh Sithivong	Savannakhet University, Laos	М	
	Somavatev Meas	Prince of Songkla University, Hat Yai		
23		Cambodian student	F	
	Chreanvutha Im	Mahasarakham University		
24		Cambodian student	M	

#### Local participants

Pisamai Kittipoom	Prince of Songkla University, Hat Yai	F
Athassawat Kammanee	Prince of Songkla University, Hat Yai	М
Worachat Imlek	Burapha University, Chonburi	М
	Kanchanaburi Rajabhat University,	
Siriwan Chankan	Kanchanaburi	F
Tharana Yosprakob	Chulalongkorn University, Bangkok	F
	King Mongkut's University of	
Dussadee Somjaiwang	Technology Thonburi, Bangkok	F
Yotsawat Terapabkajornded	Mahidol University, Bangkok	М
Somsak Orankitjaroen	Mahidol University, Bangkok	М
Chatchawan	King Mongkut's University of	
Watchararuangwit	Technology Thonburi,	М
	King Mongkut's University of	
Kanya Maleelai	Technology Thonburi,	F
	Pisamai Kittipoom Athassawat Kammanee Worachat Imlek Siriwan Chankan Tharana Yosprakob Dussadee Somjaiwang Yotsawat Terapabkajornded Somsak Orankitjaroen Chatchawan Watchararuangwit Kanya Maleelai	Pisamai KittipoomPrince of Songkla University, Hat YaiAthassawat KammaneePrince of Songkla University, Hat YaiWorachat ImlekBurapha University, ChonburiKanchanaburi Rajabhat University, KanchanaburiKanchanaburi Rajabhat University, KanchanaburiTharana YosprakobChulalongkorn University, BangkokDussadee SomjaiwangTechnology Thonburi, BangkokYotsawat TerapabkajorndedMahidol University, BangkokSomsak OrankitjaroenMahidol University, BangkokChatchawanKing Mongkut's University of Technology Thonburi, BangkokKing Mongkut's University of Technology Thonburi,Kanya MaleelaiKing Mongkut's University of Technology Thonburi,

		Phranakhon Si Ayutthaya Rajabhat	
35	Sopida Jewprasert	University, Ayutthaya	F
36	Sunee Pongpinigpinyo	Silpakorn University	F
37	Pornchanok Kummaung	Silpakorn University	F
38	Tereporn Thongsiri	Silpakorn University	М
39	Piyawat Wongthongone	Silpakorn University	М
40	Pitchaporn Paitong	Silpakorn University	F
41	Pakkapon Phongthawee	Silpakorn University	М
42	Risa Masiri	Silpakorn University	F
43	Nichanat Wiriyakaset	Silpakorn University	F
44	Sawanya Sakuntasathien	Silpakorn University	F
45	Naeem Binibroheng	Silpakorn University	М
46	Satanan Thipworawimon	Silpakorn University	F
47	Wannapa Panitsupakamon	Silpakorn University	F
48	Nairat Kanyamee	Silpakorn University	F
49	Kanyakorn Cheuprasert	Silpakorn University	F
50	Prarinya Morrakutjinda	Silpakorn University	М

#### V. School Programs

1. Scientific python

Marília Pires, PhD, University of Évora, Portugal

This practice presents the main features of a free software to solve mathematical equations derived from concrete problems. This course is done on computer.

- Presentation of python
- Basics (number, characters, function), Graphics
- Linear and nonlinear systems
- Numpy, Sympy.

#### 2. Finite difference methods for PDEs

- Noppadol Chumchob, PhD, Silpakorn University, Thailand
  - Brief overview of ordinary and partial differential equations
  - Elliptic PDE: 1D, 2D elliptic problems, Convergence theory
  - Parabolic PDE: 1D heat equation, Stability, Convergence theory for timedependent problems
  - Image processing-image restoration.
- 3. Exact solutions of smoothing PDEs

Nabil Bedjaoui, PhD, University of Picardie, France

- Separation of variables, Fourier series
- Fourier transform

Fernando da Costa, PhD, University Aberta, Portugal

- Convolution
- Image restoration, Filtering.

4. Hyperbolic PDEs

Nabil Bedjaoui, PhD, University of Picardie, France

- Linear and nonlinear models (transport, waves and optics, dissipation and dispersion)
- Joaquim Correia, PhD, University of Évora, Portugal
  - Dynamics of image processing & parabolic-hyperbolic models
  - Image denoising and restoration & viscosity solutions, shock capturing
  - Image segmentation and the Level Set Method & characteristics, weak solutions
  - Curves and signals & metrics, dynamic geometry and scales.
- 5. Computer implementation of PDEs

Youcef Mammeri, PhD HDR, University of Picardie, CNRS, INRA, France This lecture is dedicated to the implementation of methods presented in the other lectures. This course is done on computer.

- Scipy routines for image manipulation
- Fast Fourier Transform, Convolution, Filtering
- Finite differences implementation, Denoising, Inpainting.

DAY TIME	WEDNESDAY 01/03	THURSDAY 01/04	Friday 01/05	SATURDAY 01/06	SUNDAY 01/07
8:00-8:30	Opening				
8:30-10:15	Noppadol	Noppadol	Noppadol		
10:15- 10:45	break	break	break		
10:45- 12:15	Bedjaoui	Bedjaoui	Costa	Excursion	Free
12:30- 14:00	lunch	lunch	lunch	everybody	Titte
14:00- 15:30	Pires	Pires	Pires		
15:30- 17:30	group discussions	group discussions	group discussions		

Welcome Dinner

DAY TIME	Monday 01/08	TUESDAY 01/09	Wednesday 01/10	THURSDAY 01/11	Friday 01/12
8:30-10:15	Noppadol	Bedjaoui	Correia	Correia	Correia
10:15-10:45	break	break	break	break	break
10:45-12:15	Costa	Pires	Mammeri	Mammeri	group discussions
12:30-14:00	lunch	lunch	lunch	lunch	Closing
14:00-15:30	Pires	Mammeri	group discussions	Mammeri	lunch
15:30-17:30	group discussions	group discussions	Testimony	group discussions	

Each day was concluded by group discussions. Students were split in six groups composed by different (training and) countries and were working together to solve exercises given by the lecturers. Besides the exercises, 13.5 hours of classes were held on computer within a large room (1 computer per student) and two screens for simultaneous projection.

Saturday 06 January, everybody enjoys a full day of excursion inside the Chaipattana Career Park, the Don Wai Floating Market, the Molding factory of Prof. Mana Taiwuttanakul and the Phra Pathom chedi.

#### VI. Conclusion

According the opinion of participants, staff, teachers, lecturers and organizers, this SEAMS School was a great success. Participants had an overview of the importance of the theoretical and numerical basis to handle image (computer) processing through partial differential equations.

The testimony was an opportunity to learn more about the expectations and sentiments of the students. The distribution of the courses was appreciated and the 10-days school was considered a bit short by the students.

The gender balance in terms of participants was respected (50% of female). The budget was met.

It was a great opportunity for students of the region to meet each other and we wish they will collaborate in the future (this has been explicitly stated by the organizers and lecturers has a major goal of SEAMS schools).

This school has also been prolific for teachers. It has strengthened the links with Thailand both in terms of future training and in terms of research. Two days after the school, a meeting was organized with representatives of Silpakorn University (Thailand), Birla Institute of Technology & Science of Pilani (India), Quy Nhon University (Vietnam), National University of Laos (Laos), University of Évora (Portugal) and University of Picardie (France).

J. Correia, M. Pires, and Y. Mammeri stayed in the Silpakorn University to pursue the lectures and preparing international projects applications.

#### VII. Financial Report

See appendix for details.

We would like to mention that it would not have been possible to host so many foreign participants without the immense support of the Silpakorn University which, in addition to supporting 5 rooms for Thai participants, has financed another 5 rooms. We would also like to thank Caraga State University for taking over the transport between Butuan and Manila for the two Philippines participants.